## **Ordering tendencies in octahedral MgO-ZnO alloys**

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Isostructural II-VI alloys whose components are either rocksalt stable (e.g., CaO-MgO) or zincblende stable ~e.g., ZnS-ZnSe! are known to be thermodynamically unstable at low temperatures, showing a miscibility gap and no bulk ordering. In contrast, we show that *heterostructural* MgO-ZnO is stable, under certain conditions, in the sixfold-coordinated structure for Zn concentrations below 67%, giving rise to spontaneously ordered alloys. Using first-principles calculations, we explain the origin of this stability, the structures of their lowtemperature ordered phases, short-range-order patterns, and their optical band-gap properties.

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## **I. INTRODUCTION**

Binary II-VI compounds appear<sup>1</sup> largely as fourfoldcoordinated  $(CN4)$  zincblende/wurtzite structures  $(ZnO,$ ZnS, ZnSe, ZnTe, CdS, CdSe, and CdTe) or as sixfoldcoordinated (CN6) rocksalt structures (MgO, CaO, and CdO). Isovalent and isostructural alloys of II-VI constituents are generally thermodynamically unstable, in that their mixing enthalpy, in either the CN6 rocksalt (*B*1) structure or in the CN4  $(B3)$  or wurtzite  $(B4)$  structures,

$$
\Delta H_{\alpha}(A_x B_{1-x}C) = E_{\alpha}(A_x B_{1-x}C) - [xE_{\alpha}(AC)
$$

$$
+ (1-x)E_{\alpha}(BC)], \tag{1}
$$

is *positive*.<sup>2-4</sup> Here,  $\alpha$  denotes fourfold or sixfold coordinated crystal structure, and  $E_{\alpha}(AC)$ 

functional for  $\sim$  3 $\times$  10<sup>6</sup> possible configurations, we identify  $Mg_3ZnO_4$  ( $DO_{22}$ ) and  $Mg_4Zn_4O_8$  as ordered *B*1-like ground-state structures.  $(5)$ 

are the most stable. To answer this we have parametrized 32 *B*1 total-energy calculations of  $Mg_mZn_nO_{m+n}$  structures  $(s$ hown as open squares in Fig. 2) into a cluster expansion. Within the cluster-expansion method<sup>7</sup> one selects an underdictions within 0.3 meV/atom. Although several ''breaking points'' exist, the energetically ''deepest'' structures occur at  $x=0.25$  and  $x=0.5$ . For  $x=0.25$ , the ground state is a  $D0_{22}$ -type structure with lattice constants  $a=4.174$  Å and  $c=4.179$  Å. For  $x=0.50$ , the ground state is an orthorhombic structure with lattice constants  $a=4.189 \text{ Å}$ , *b*  $=$  4.187 Å, and  $c = 8.900$  Å. The atomic positions and lattice vectors of predicted ground states are shown in Table III. The common structural motif for these ground-state structures is that they are  $(201)$  superstructures. It is known that  $(201)$ superstructures have low Madelung energies<sup>7</sup> and our calculations show that the constituent strain energy along the  $(201)$  direction is softer with respect to the other principal directions.

## **C. Thermodynamic modeling**

Figure 2 shows the energy of the random *B*1 solid solutions (solid line), obtained by performing high-temperature (40 000 K) Monte Carlo simulations with Hamiltonian,  $E_{\text{CE}}($  ). The open symbols denote the energies of ordered structures, used as input to the cluster expansion, whereas the energies of the ground-state structures are denoted by solid squares. We see that the energy difference between the stable ordered ground-state structures and the random alloy of the same composition (e.g.,  $x=0.5$ ) is rather small ( $-6.5$  meV/ cation), so the order-disorder transition temperature will be well below conventional growth th tol 2s6 1 Tf .443 Tm (s)Tj /F8 1 T0cc e.g., (a) sabsolution temperature will be<br>(b) 1 or 443 Tm (s)Tj /F8 1 T0cc<br>(b) 77n48e5.D (~)ss 25Tj /6.0445 1 Tf all<br>(b)  $\frac{1}{2}$ 

O77n48e5.D (~)ss 25Tj /6.0445 1 Tf al

at high temperatures. The random alloy has an LDA band gap of 2.49 eV at  $x=0.5$  (using a special quasirandom structure<sup>17</sup>), and hence a bowing coefficient  $b_{\text{bowing}}$  $= 3.10 \text{ eV}, \text{ where } E_g(x) = (1-x)E_{\text{MgO}} + xE_{\text{ZnO}} - x(1)$  $(x-x)b_{\text{bowing}}$ . This value of the bowing coefficient is in good agreement with the value of  $3.6\pm0.6$  eV measured recently by Schmidt *et al.*<sup>10</sup> The ordered structure at  $x=0.5$  has a lower band gap than the random alloy by 0.39 eV. There is a CN6 to CN4 transition for  $x_{Zn} > 0.67\%$ , whereas the coherent alloy is *B*1 stable below this composition. If MgO and ZnO can (incoherently) adopt their own crystal structures  $(B1 \text{ and } B4, \text{ respectively})$ , the alloy is predicted to phase separate.

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